

**Relativity:**  $\beta = \frac{v}{c}$      $\gamma = \frac{1}{\sqrt{1-\beta^2}}$      $t' = \gamma t_0$      $L = L_0/\gamma$      $x' = \gamma(x - vt)$   
 $y' = y$      $z' = y$      $t' = \gamma(t - \beta x/c)$      $\Delta s^2 = \Delta x^2 - c^2 \Delta t^2$   
 $u_x = \frac{u'_x + v}{1 + vu'_x/c^2}$      $u_y = \frac{u'_y}{\gamma(1 + vu'_x/c^2)}$      $u_z = \frac{u'_z}{\gamma(1 + vu'_x/c^2)}$      $f = \frac{\sqrt{1+\beta}}{\sqrt{1-\beta}} f_0$   
 $\vec{p} = \gamma m \vec{u}$      $K = (\gamma - 1)mc^2$      $E^2 = (pc)^2 + (mc^2)^2$

**Early Quantum Theory:**  $\frac{1}{\lambda} = R_H \left( \frac{1}{n^2} - \frac{1}{k^2} \right)$      $\lambda_{max} T = 2.989 \times 10^{-3} \text{ m} \cdot \text{K}$   
 $R(T) = \epsilon \sigma_{SB} T^4$      $I(\lambda, T) = \frac{2\pi c^2 h}{\lambda^5} \frac{1}{e^{hc/\lambda k_B T} - 1}$      $E = hf = \frac{hc}{\lambda}$   
 $hf = \phi + \frac{1}{2} m v_{max}^2$      $\lambda_{min} = \frac{hc}{eV_0}$      $\Delta \lambda = \frac{hc}{mc^2} (1 - \cos \theta)$

**Atomic Structure:**  $\alpha = \frac{k_e e^2}{\hbar c} \approx \frac{1}{137}$      $a_0 = \frac{\hbar^2}{m k_e e^2} = \frac{1}{\alpha} \frac{\hbar c}{m c^2}$      $\mu = \frac{mM}{m+M}$   
 $R_H = \frac{\mu}{m_e} R_\infty$      $E_0 = \frac{m k_e^2 e^4}{2\hbar^2} = \frac{k_e e^2}{2a_0} \approx 13.6 \text{ eV}$      $E_n = -\frac{Z^2 E_0}{n^2}$

**Waves:**  $\lambda = \frac{h}{p}$      $k = \frac{2\pi}{\lambda}$      $v_p = \frac{\omega}{k}$      $v_g = \frac{d\omega}{dk}$      $\Delta p \Delta x \geq \frac{\hbar}{2}$      $\Delta E \Delta t \geq \frac{\hbar}{2}$   
 $P(x) dx = \psi(x)^* \psi(x) dx$      $E_n = n^2 \frac{(hc)^2}{8mc^2 L^2}$

**Quantum Theory:**  $-\frac{\hbar^2}{2m} \frac{\partial^2 \Psi(x, t)}{\partial x^2} + V(x) \Psi(x, t) = E \Psi(x, t)$      $\Psi(x, t) = \psi(x) e^{-i\omega t}$   
 $-\frac{\hbar^2}{2m} \frac{d^2 \psi(x)}{dx^2} + V(x) \psi(x) = E \psi(x)$      $1 = \int_{-\infty}^{\infty} \psi^*(x) \psi(x) dx$      $\hat{p} = \frac{\hbar}{i} \frac{\partial}{\partial x}$   
 $\langle A \rangle = \int_{-\infty}^{\infty} \psi^*(x) \hat{A} \psi(x) dx$      $E_n = n^2 \frac{\hbar^2}{8mL^2}$      $E_n = (n + \frac{1}{2}) \hbar \omega$   
 $\kappa = \frac{\sqrt{2m(V_0 - E)}}{\hbar}$      $T = 16 \frac{E}{V_0} \left( 1 - \frac{E}{V_0} \right) e^{-2\kappa L}$

**Hydrogen Atom:**  $V = -\frac{k_e e^2}{r}$      $\psi(r, \theta, \phi) = R_{nl}(r) Y_{lm_l}(\theta, \phi)$      $E_n = -\frac{E_0}{n^2}$   
 $E_0 = 13.6 \text{ eV}$      $P(r) = |R(r)|^2 r^2 dr$      $L = \sqrt{l(l+1)} \hbar$      $L_z = m_l \hbar$      $\vec{\mu} = -\frac{e}{2m} \vec{L}$   
 $\mu_B = \frac{e\hbar}{2m}$      $V_B = -\mu_z B = +\mu_B m_l B$

**Constants:**  $e = 1.602 \times 10^{-19} \text{ C}$      $m_e = 9.11 \times 10^{-31} \text{ kg}$      $c = 2.998 \times 10^8 \text{ m/s}$   
 $m_e c^2 = 0.511 \text{ MeV}$      $m_p c^2 = 938.27 \text{ MeV}$      $m_n c^2 = 939.57 \text{ MeV}$   
 $k_e = 8.9876 \times 10^9 \text{ Nm}^2/\text{C}^2$      $h = 6.626 \times 10^{-34} \text{ Js}$      $\hbar = 1.055 \times 10^{-34} \text{ Js}$   
 $hc = 1239.8 \text{ eV} \cdot \text{nm}$      $k_B = 1.3807 \times 10^{-23} \text{ J/K}$      $R_\infty = \frac{\alpha^2 m_e c^2}{2hc} = 0.0109737 \text{ nm}^{-1}$   
 $R_H = 0.0109678 \text{ nm}^{-1}$      $1 \text{ u} = 931.5 \text{ MeV}/c^2 = 1.66 \times 10^{-27} \text{ kg}$      $1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$   
 $a_0 = 0.0529 \text{ nm}$      $\mu_B = 5.7884 \times 10^{-5} \text{ eV/T}$      $\sigma_{SB} = 5.6704 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$