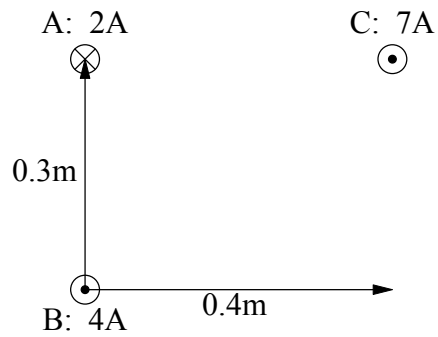
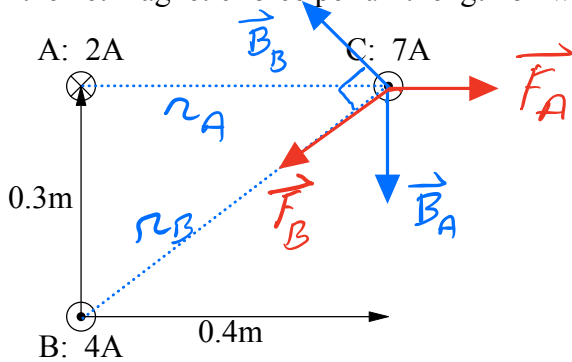


2. (20 pts.) Three long parallel wires are arranged as shown. Wire A has a current of 2A headed into the page, wire B has a current of 4A headed out of the page, and wire C has a current of 7A headed out of the page, as shown. Find the magnitude and direction of the net magnetic force per unit length on wire C.



2. (20 pts.) Three long parallel wires are arranged as shown. Wire A has a current of 2A headed into the page, wire B has a current of 4A headed out of the page, and wire C has a current of 7A headed out of the page, as shown. Find the magnitude and direction of the net magnetic force per unit length on wire C.



$$r_A = 0.4m$$

$$r_B = \sqrt{(0.3m)^2 + (0.4m)^2}$$

$$r_B = 0.5m$$

$\vec{B}_A$  = magnetic field due to wire A at wire C.

$$\vec{B}_A = \frac{\mu_0 I_A}{2\pi r_A}, \text{ down. } \left( \vec{B}_A \text{ goes in a clockwise circle around wire A.} \right)$$

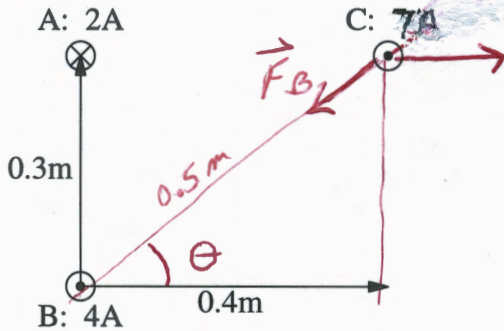
$\vec{B}_B$  = magnetic field due to wire B at wire C.

$$\vec{B}_B = \frac{\mu_0 I_B}{2\pi r_B}, \text{ up and left. } \left( \vec{B}_B \text{ goes in a counterclockwise circle around wire B.} \right)$$

$$\vec{F}_A = I_C \vec{L}_C \times \vec{B}_A \Rightarrow \frac{\vec{F}_A}{L_C} = I_C B_A, \text{ right.}$$

$$\vec{F}_B = I_C \vec{L}_C \times \vec{B}_B \Rightarrow \frac{\vec{F}_B}{L_C} = I_C B_B, \text{ down and left.}$$

2. (20 pts.) Three long parallel wires are arranged as shown. Wire A has a current of 2A headed into the page, wire B has a current of 4A headed out of the page, and wire C has a current of 7A headed out of the page, as shown. Find the magnitude and direction of the net magnetic force per unit length on wire C.



$$\tan \theta = \frac{.3}{.4}$$

$$\theta = 36.9^\circ$$

$$\frac{\vec{F}_A}{L_C} = \frac{\mu_0 I_A I_C}{2\pi r_{AC}} \quad \text{①} \quad 0^\circ, \quad I_A = 2, I_C = 7, r_{AC} = 0.4$$

$$\frac{\vec{F}_B}{L_C} = \frac{\mu_0 I_B I_C}{2\pi r_{BC}} \quad \text{②} \quad (180^\circ + 36.9^\circ = 216.9^\circ)$$

$$I_B = 4A, I_C = 7A, r_{BC} = 0.5$$

$$\vec{F}_{TOT} = \vec{F}_A + \vec{F}_B$$

x-components

$$\frac{F_{TOT,x}}{L_C} = \frac{F_{Ax}}{L_C} + \frac{F_{Bx}}{L_C} = \frac{\mu_0 I_A I_C}{2\pi r_{AC}} + \frac{\mu_0 I_B I_C}{2\pi r_{BC}} \cos 216.9$$

$$= \frac{\mu_0 I_C}{2\pi} \left[ \frac{I_A}{r_{AC}} + \frac{I_B}{r_{BC}} \cos 216.9 \right]$$

$$= \frac{(4\pi \times 10^{-7})(7)}{2\pi} \left[ \frac{2}{.4} + \frac{4}{.5} \cos 216.9 \right] = -1.96 \times 10^{-6} \text{ N}$$

$$\frac{F_{TOT,y}}{L_C} = \frac{F_{Ay}}{L_C} + \frac{F_{By}}{L_C} = 0 + \frac{\mu_0 I_B I_C}{2\pi r_{BC}} \sin 216.9 = \frac{(4\pi \times 10^{-7})(4)(7)}{2\pi(.5)} (-0.6)$$

$$= -6.72 \times 10^{-6} \text{ N}$$

$$\boxed{\frac{F_{TOT}}{L_C} = 7.0 \times 10^{-6} \text{ N} \quad \text{③} \quad -106^\circ}$$