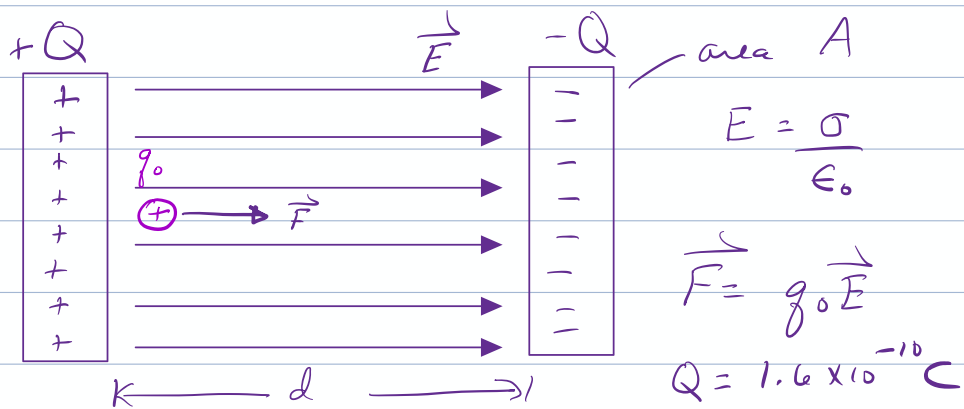


21.4 Calculating the Electric Potential and 21.3 Conservation of Energy

Plan: Calculate ΔU , then $\Delta V = \frac{\Delta U}{q_0}$.
 We will consider 2 basic settings, the parallel plate capacitor and a point charge.

Parallel Plates:



Problem: Consider two square plates, 10 cm on a side, separated by a distance of 5 mm. Imagine a proton is released from rest at the + plate. How quickly is it moving when it reaches the - plate?

Way #1 $F = ma$

$$qE = ma \Rightarrow a = \frac{qE}{m}$$

$$E = \frac{\sigma}{\epsilon_0} = \frac{Q/A}{\epsilon_0} = \frac{(1.6 \times 10^{-10} \text{ C}) / (0.10 \text{ m})^2}{8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2}$$

$$E = 1807 \text{ N/C}$$

$$\text{Then } a = \frac{(1.602 \times 10^{-19} \text{ C})(1807 \text{ N/C})}{1.6726 \times 10^{-27} \text{ kg}}$$

$$a = 1.731 \times 10^{11} \text{ m/s}^2 \quad (\text{huge!})$$

$$\text{Kinematics: } v_f^2 = v_i^2 + 2ad$$

$$v_f^2 = 0 + 2ad$$

$$v = \sqrt{2ad} = \sqrt{2(1.731 \times 10^{11} \text{ m/s}^2)(0.005 \text{ m})}$$

$$v = 41,600 \text{ m/s.}$$

Way #2 Work/Energy

$$K_i + W = K_f$$

$$\frac{1}{2} m v_i^2 + F \cdot d = \frac{1}{2} m v_f^2$$

$$\frac{1}{2} m v_i^2 + (qE) \cdot d = \frac{1}{2} m v_f^2$$

$$0 + qE d = \frac{1}{2} m v_f^2$$

$$v_f = \sqrt{\frac{2(qEd)}{m}}$$

$$v_f = \sqrt{\frac{2(1.602 \times 10^{-19} \text{ C})(1807 \text{ N/C})(0.005 \text{ m})}{1.6726 \times 10^{-27} \text{ kg}}}$$

$$v_f = 41,600 \text{ m/s.}$$

Way #3 Conservation of Energy

$$K_i + U_i = K_f + U_f$$

$$K_i + qV_i = K_f + qV_f$$

$$K_i - q(V_f - V_i) = K_f$$

compare to last

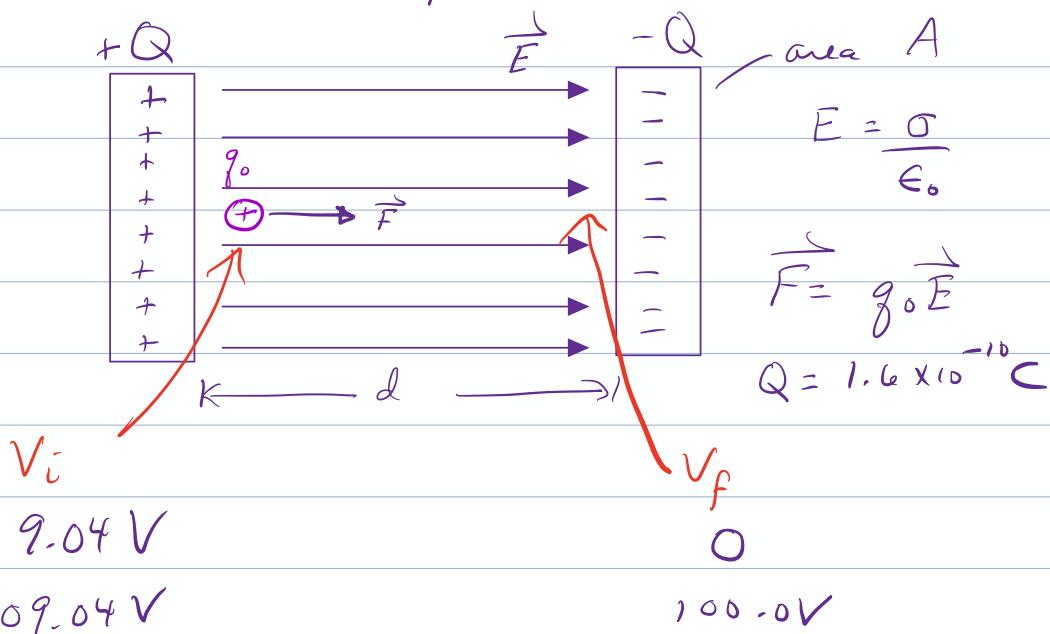
approach $K_i + q(Ed) = K_f$

This suggests $-\Delta V = Ed$ in this problem.

$$-(V_f - V_i) = (1807 \text{ N/C}) \cdot (0.005 \text{ m})$$

$$-(V_f - V_i) = 9.04 \text{ V}$$

$$V_f - V_i = -9.04 \text{ V}$$

$$V_f = V_i - 9.04 \text{ V}$$


only the difference matters

SO: For the parallel plate
 $|\Delta V| = E \cdot d$ - Sign?
 \vec{E} points from high V to low V .

So how to solve the problem?

$$K_i + U_i = K_f + U_f$$

$$K_i + qV_i = K_f + qV_f$$

$$K_i + q_i (V_i - V_f) = K_f$$

$$-\Delta V = E \cdot d = \frac{\sigma}{\epsilon_0} \cdot d = \frac{Q/A}{\epsilon_0} \cdot d$$

$$-\Delta V = \frac{(1.6 \times 10^{-10} \text{ C}) / 0.01 \text{ m}^2}{8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2} \cdot 0.005 \text{ m}$$

$$-\Delta V = 9.04 \text{ V}$$

$$-(V_f - V_i) = 9.04 \text{ V}$$

$V_i - V_f = 9.04 \text{ V}$. e^- starts at higher voltage, and travels to lower voltage.

$$\therefore K_i + q (9.04 \text{ V}) = K_f$$

$$0 + \underbrace{(e)(9.04 \text{ V})}_{9.04 \text{ eV}} = \frac{1}{2} m v_f^2$$

$$\approx (1.602 \times 10^{-19} \text{ C})(9.04 \text{ V})$$

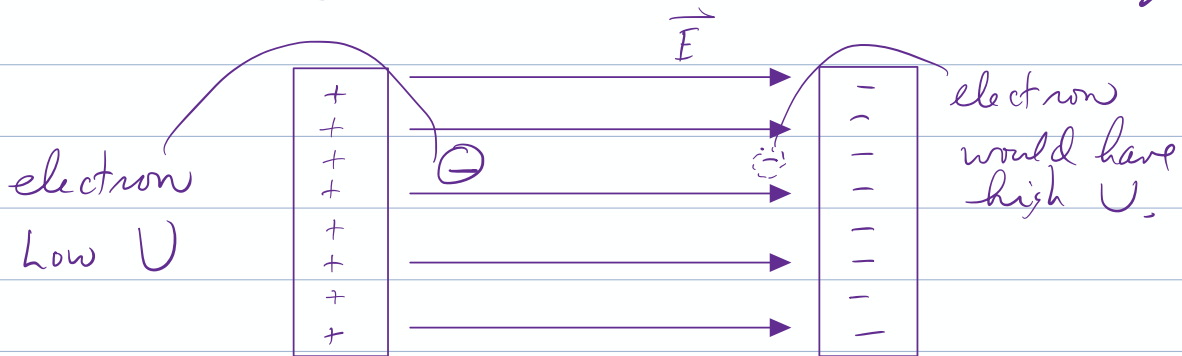
$$= 1.448 \times 10^{-18} \text{ J} = \frac{1}{2} m v_f^2$$

$$v_f = \sqrt{\frac{2 e (9.04 \text{ V})}{1.6726 \times 10^{-27} \text{ kg}}} = \underline{\underline{41,600 \text{ m/s}}}$$

Summary: for parallel plates
 $|\Delta V| = Ed$.

What if you have an electron?

$U = (-e)V$. otherwise do the same thing.

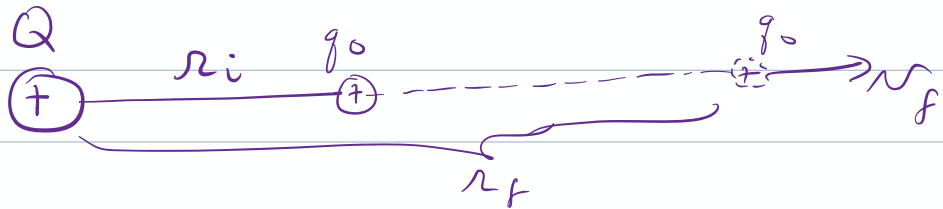


$$K_i + U_i = K_f + U_f$$

$$U = (-e)(V)$$

See examples Ch21-Energy-2 and Ch21-Energy-3.

Next: Calculating ΔV for a point charge
 e.g. have a test charge q_0 near a point charge Q :



If you release q_0 from rest it will be repelled from Q . The electric force will do work and give the particle kinetic energy at r_f .

How much work? (Not just $F \cdot d = qE \cdot d$, since the force is not constant.)

Result for a point charge Q .

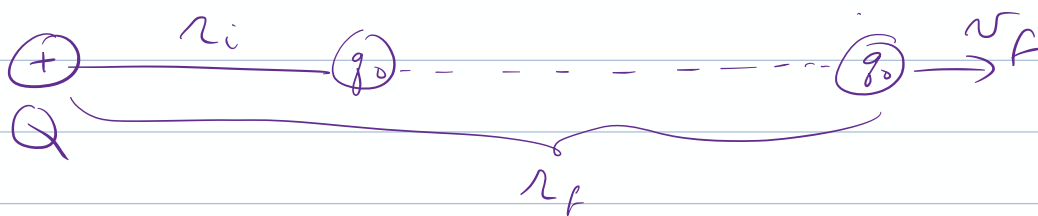
$$\vec{E} = \frac{K|Q|}{r^2}, \text{ away from } + \text{ charge,} \\ \text{towards } - \text{ charge.}$$

get $V = \frac{KQ}{r}$. Not a vector; include the sign.

Convention: take $V = 0$ when charge q_0 is ∞ far away. ($V \rightarrow 0$ as $r \rightarrow \infty$).

and $U = q_0 V = \frac{KQq_0}{r}$.

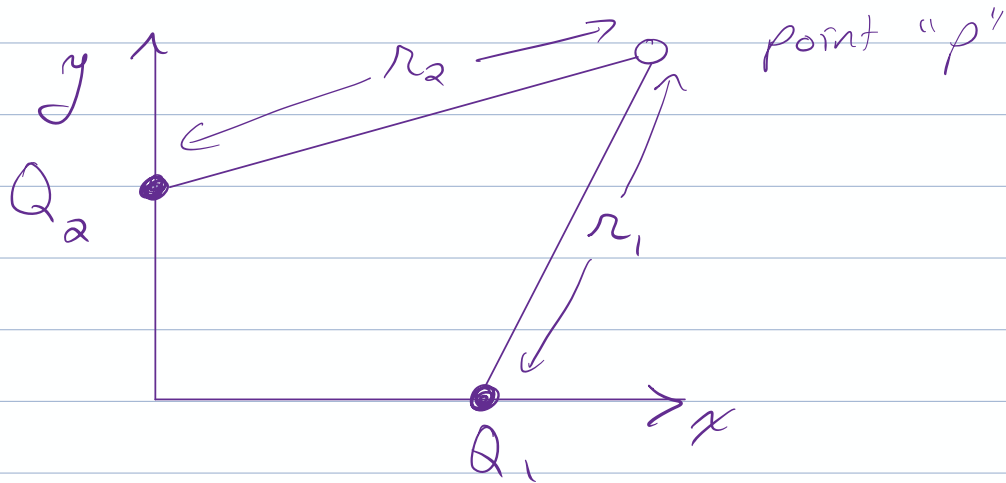
\therefore Basic structure of the problem:



$$K_i + U_i = K_f + U_f \\ \frac{1}{2} m v_i^2 + q_0 \left(\frac{KQ}{r_i} \right) = \frac{1}{2} m v_f^2 + q_0 \left(\frac{KQ}{r_f} \right)$$

See example Ch21-Energy-1

Superposition



$$V = \frac{kQ_1}{r_1} + \frac{kQ_2}{r_2}$$

No vectors!
Include signs!

Put a charge q_0 down at "p" and

$$U = q_0 V = \frac{kQ_1 q_0}{r_1} + \frac{kQ_2 q_0}{r_2}$$

See Ch 21 - superposition - 1. pdf.