

5. (30 pts.) A satellite of mass 220kg is initially in a circular orbit of radius $7.31 \times 10^6\text{m}$ (measured from the **center** of the earth).

- a. (10 pts.) Find the speed of the satellite.
- b. (10 pts.) Find the total mechanical energy of the satellite.
- c. (10 pts.) Due to friction with the earth's atmosphere, the satellite slowly spirals in towards the earth. Suppose that at some later time, the satellite is in a circular orbit of radius $6.90 \times 10^6\text{m}$ (measured from the **center** of the earth). Assume that the orbit is circular.

Is the new total mechanical energy greater than, less than, or equal to the initial total mechanical energy? Justify your answer.

$$M_E = 5.98 \times 10^{24}\text{kg}$$

$$R_E = 6.37 \times 10^6\text{m}$$

4. (30 pts.) A satellite of mass 220 kg is initially in a circular orbit of radius 7.31×10^6 m (measured from the center of the earth).

- (10 pts.) Find the speed of the satellite.
- (10 pts.) Find the total mechanical energy of the satellite.
- (5 pts.) Due to friction with the earth's atmosphere, the satellite slowly spirals in towards the earth. Suppose that at some later time, the satellite is in a circular orbit of radius 6.90×10^6 m (measured from the center of the earth). Find the new speed of the satellite. (Assume that the orbit is circular.)
- (5 pts.) Is the new total mechanical energy greater than, less than, or equal to the initial total mechanical energy? Justify your answer.

$$a. F = ma \Rightarrow \frac{GMm}{r^2} = \frac{mv^2}{r} \Rightarrow v = \sqrt{\frac{GM_E}{r}} = \boxed{7387 \text{ m/s}}$$

$$b. K = \frac{1}{2}mv^2 = \frac{1}{2}(220 \text{ kg})(7387 \text{ m/s})^2 = 6.00 \times 10^9 \text{ J}$$

$$U = \frac{-GMm}{r} = \frac{-(6.67 \times 10^{-11})(5.98 \times 10^{24})(220)}{7.31 \times 10^6} = -1.200 \times 10^{10} \text{ J}$$

$$E = K + U = \boxed{-6.00 \times 10^9 \text{ J}}$$

$$c. v = \sqrt{\frac{GM_E}{r}} = \sqrt{\frac{(6.67 \times 10^{-11})(5.98 \times 10^{24})}{6.90 \times 10^6}} = \boxed{7603 \text{ m/s}}$$

speed goes up!

$$d. K = \frac{1}{2}mv^2 = 6.36 \times 10^9 \text{ J}$$

$$U = \frac{-GMm}{r} = -1.27 \times 10^{10} \text{ J}$$

$$E = \boxed{-6.36 \times 10^9 \text{ J}}$$

Note: speed goes up, but total energy goes down.