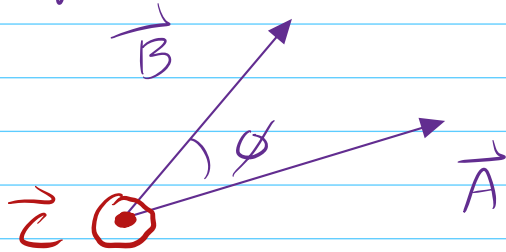


The cross product is discussed in Chapter 1, Section 10.

define: $\vec{C} = \vec{A} \times \vec{B}$ to mean



$$|\vec{C}| = |\vec{A}| |\vec{B}| \sin \phi$$

$$\text{direction: } \vec{C} \perp \vec{A}, \vec{B} \text{ plane}$$

Right Hand Rule (many ways to express this - here is my favourite:)

- ① Place right hand fingers along \vec{A} .
- ② Rotate or curl them to point along \vec{B} .
- ③ Thumb points along \vec{C} .

Special cases

$$\vec{A} \perp \vec{B} ? \sin \phi = 1, \quad C = AB$$

$$\vec{A} \parallel \vec{B} ? \sin \phi = 0, \quad C = 0.$$

Anti-symmetry: order matters

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$$

Unit vectors:

$$\hat{i} \times \hat{j} = \hat{k}$$

$$\hat{j} \times \hat{k} = \hat{i}$$

$$\hat{k} \times \hat{i} = \hat{j}$$

(note, all in order
 $i j k \quad i j k \dots$)

This also leads to a vector component version.
(assume \vec{A} and \vec{B} are in $x-y$ plane for simplicity)

$$\vec{A} \times \vec{B} = (A_x \hat{i} + A_y \hat{j}) \times (B_x \hat{i} + B_y \hat{j})$$

expand term-by-term, keeping in order

$$\vec{A} \times \vec{B} = A_x B_x \underbrace{\hat{i} \times \hat{i}}_0 + A_x B_y \underbrace{\hat{i} \times \hat{j}}_{\hat{k}}$$
$$+ A_y B_x \underbrace{\hat{j} \times \hat{i}}_{-\hat{k}} + A_y B_y \underbrace{\hat{j} \times \hat{j}}_0$$

$$\vec{A} \times \vec{B} = (A_x B_y - A_y B_x) \hat{k} \quad (\vec{A}, \vec{B} \text{ in } x-y \text{ plane})$$

(full 3-D, see Eq 1.24 in Ch. 1.)

So here

$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$\vec{\tau} \text{ is } \perp \vec{r}, \perp \vec{F}, \quad \tau = r F \sin \phi.$$