

Fermi-Dirac Distribution

```
In[41]:= Clear["Global`*"]
```

Use the Fermi-Dirac distribution.

```
In[42]:= nFD[ε_, μ_, T_] := 
$$\frac{1}{\text{Exp}[(\epsilon - \mu) / (k T)] + 1}$$
 // Quiet
```

The chemical potential can be found by the normalization condition, $N = \int_0^\infty n(E) dE$. For a typical free electron gas model of a conductor, a value of 5 eV is reasonable. Use that for an illustrative graph. For extreme ranges, Mathematica issues warnings about loss of precision. We will ignore them here since they don't impact our qualitative results here.

```
In[43]:= k = QuantityMagnitude[
  UnitConvert[Quantity[1., "BoltzmannConstant"], "Electronvolts"/"Kelvins"]]
(* Boltzmann's Constant in eV/K *)
```

```
Out[43]=
0.0000861733
```

```
In[44]:= μ = 5.00; (* in eV *)
```

This plot shows the FD distribution for different temperatures, and keeps the very-low temperature graph on for comparison.

```
In[45]:= N[nFD[5, μ, 1]]
```

```
Out[45]=
0.5
```

```
In[52]:= Manipulate[Plot[{nFD[ε, μ, 0.1], nFD[ε, μ, T]}, {ε, 0, 10},  
  LabelStyle → Larger, AxesLabel → {"ε (eV)", "nFD"},  
  PlotLegends → {"Low T", StringForm["T = ` ` (K)", T]},  
  PlotRange → {{0, 10}, {0, 1}}, ImageSize → Scaled[0.7]] // Quiet,  
{T, 10, 10000, Appearance → "Open"}]
```

Out[52]=

